

# LAST MIPS LECTURE REDO

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## LECTURE 10-1

JIM FIX, REED COLLEGE CS2-S20

## TODAY'S PLAN

A "REDO" OF THE SECOND HALF OF LAST WEDNESDAY

- ▶ LINKED LIST MIPS CODE
- ▶ **SHIFTING** A REGISTER'S BITS LEFT AND RIGHT
- ▶ MULTIPLICATION USING BASE TWO "SCHOOLBOOK METHOD"
- ▶ **CALL STACK AND CALLING CONVENTIONS**

## THIS WEEK

- ▶ **HOMEWORK 09 ASSIGNED TONIGHT, DUE NEXT MONDAY.**
- ▶ **NO LABS TOMORROW.** (Happy election day.)
- ▶ WILL HOLD OFFICE HOURS 9:30-10:30, 3:30-4:30. (See the Slack.)
- ▶ **WEDNESDAY'S LECTURE WILL BE OVER ZOOM ONLY**

## TRaversING A LINKED LIST

### ► MIPS code that outputs a linked list

```
1. print:
2.     move    $s1, $s0           # current = first;
3. print_loop:
4.     beqz   $s1, done          # if current==nullptr goto done;
5. print_data:
6.     lw     $a0, ($s1)         # print(current->data);
7.     li    $v0, 1
8.     syscall
9.     lw     $s1, 4($s1)        # current = current->next;
10.    b     print_loop
11. done:
```

### ► Check out my sample "inorder.s" that builds a linked list in sorted order.

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### ► Check out my sample "inorder.s" that builds a linked list in sorted order.

## SAMPLE MIPS: INORDER.S

- ▶ This starting code sets up the data for 6 linked list nodes

```

        .data
next:    .asciiz "next\n"
eoln:    .asciiz "\n"
num_nodes: .word 6
nodes:   .word 35, 0x0000, 6, 0x0000, 17, 0x0000,
           3, 0x0000, 132, 0x0000, 20, 0x0000

        .globl main
        .text

```

- ▶ It then uses \$a1 to point to the first, and scans through the rest using \$a2.

```

main:
        la      $a1, nodes          # first = the first node
        addi   $a2, $a1, 8          # others = first + (8 bytes)
        lw     $a3, num_nodes       #
        addi   $a3, $a3, -1         # to_insert = num_nodes-1
insert_each:
        beqz   $a3, done_insert    # if to_insert == 0 goto done_insert

```

- ▶ We use \$a3 to keep track of how many items still need to be inserted.

## SAMPLE MIPS: INORDER.S

- ▶ This sets up \$t3 to hold data for a value to be inserted

```
insert_in_order:
    lw      $t3, ($a2)      # load node->data
```

- ▶ This sets up \$t4 and \$t5 as list traversal pointers. Then we scan the list for the insertion place.

```
    move    $t4, $a1      # curr = first
    li      $t5, 0x0000   # prev = null
find_place:
    beqz    $t4, insert   # if curr == nullptr go to insert
    lw      $t6, ($t4)    # load curr->data
    ble     $t3, $t6, insert # if node->data < curr->data
                                     # go to insert
    move    $t5, $t4      # prev = curr
    lw      $t4, 4($t4)   # curr = curr->next
    b       find_place
```

## SAMPLE MIPS: INORDER.S

- ▶ In the code below we either update **first**, or update **prev->next**

**insert:**

```

    addi    $a3, $a3, -1           # to_insert -= 1
    sw      $t4, 4($a2)           # node->next = curr
    beqz    $t5, insert_in_front  # if prev == nullptr
                                           # go to insert_at_front

```

**insert\_middle:**

```

    sw      $a2, 4($t5)           # prev->next = node
    b      bump_node

```

**insert\_in\_front:**

```

    move    $a1, $a2             # first = node

```

- ▶ This code advances our pointer within the nodes array within **.data**.

**bump\_node:**

```

    addi    $a2, $a2, 8           # node = next node in the node array
    b      insert_each

```



## MULTIPLICATION

- ▶ Consider these two expressions

```
return 10 * tens + ones;
```

```
return 100 * number;
```

- ▶ Q: How do we perform those multiplications in MIPS?

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- ▶ A2: Use the MIPS **MULT** instruction, along with **MFLO** and **MFHI**

## MULTIPLICATION

- ▶ Consider these two expressions

```
return 10 * tens + ones;
```

```
return 100 * number;
```

- ▶ Q: How do we perform those multiplications in MIPS?
- ▶ A1: Repeated addition. *Not how multiplication is performed. Too slow.*
- ▶ A2: Use the MIPS **MULT** instruction, along with **MFLO** and **MFHI**
- ▶ A3: That's probably the best way. But let's consider a third way...

## ANSWER 3: USE BIT SHIFTING OPERATIONS

- ▶ Using built-in multiplication is fine, but there is another way, too.
- ▶ **RECALL:** multiplying by two will shift the bits of a number left:

**111**     $\ll$  binary for the value 7

**1110**     $\ll$  binary for the value  $2*7=14$

**111000**     $\ll$  binary for the value  $8*7=56$

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- ▶ **NOTE:**  $10x = (2+8)x = 2x + 8x$



## ANSWER 3: USE BIT SHIFTING OPERATIONS

- ▶ Using built-in multiplication is fine, but there is another way, too.
- ▶ **RECALL:** multiplying by two will shift the bits of a number left:

111    <= binary for the value 7

1110    <= binary for the value  $2*7=14$

111000    <= binary for the value  $8*7=56$

- ▶ **Q:** So how might we multiply by 10?
- ▶ **NOTE:**  $10x = (2+8)x = 2x + 8x$
- ▶ **A:** We can multiply by 2, then by 8, and sum the two results.
- ▶ I.E...

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- ▶ **Q:** So how might we multiply by 10?
- ▶ **NOTE:**  $10x = (2+8)x = 2x + 8x$
- ▶ **A:** We can multiply by 2, then by 8, and sum the two results.
- ▶ **I.E.** We can shift left one bit and also shift left three bits. Then add.

## ANSWER 3: USE BIT SHIFTING OPERATIONS

- ▶ The code below uses the **SLL** instruction to do exactly that with t0:

```
sll  $t1,$t0,1
sll  $t2,$t0,3
addu $t0,$t1,$t2
```

## ANSWER 3: USE BIT SHIFTING OPERATIONS

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addu $t0,$t1,$t2
```

tmp = tmp \* 10

- ▶ It has the effect of multiplying t0 by 10.

## ANSWER 3: USE BIT SHIFTING OPERATIONS

- ▶ The code below uses the **SLL** instruction to do exactly that with t0:

```
sll  $t1,$t0,1
sll  $t2,$t0,3      tmp = tmp * 10
addu $t0,$t1,$t2
```

- ▶ It has the effect of multiplying t0 by 10.
- ▶ **Q:** So how might we multiply by 100?

## ANSWER 3: USE BIT SHIFTING OPERATIONS

- ▶ The code below uses the **SLL** instruction to do exactly that with t0:

```
sll  $t1,$t0,1
sll  $t2,$t0,3
addu $t0,$t1,$t2
```

tmp = tmp \* 10

- ▶ It has the effect of multiplying t0 by 10.
- ▶ **Q:** So how might we multiply by 100?
- ▶ **SAME IDEA:**  $100 = 64 + 32 + 4$
- ▶ **A:** So we shift 2, 5, and 6 places left. Add.

## MULTIPLICATION BY 100

- ▶ The code below multiplies t0 by 100:

```
sll  $t1,$t0,2
sll  $t2,$t0,5
sll  $t3,$t0,6
addu $t0,$t1,$t2
addu $t0,$t0,$t3
```

## SHIFTING BITS LEFT (LOGICAL)

SHIFT A REGISTER'S BITS **LEFT** SOME NUMBER OF POSITIONS

**SLL** *destination, positions*

### ► NOTES:

- This is a "shift logical value left"
- The bits of the ***destination*** are shifted left, with the leftmost bits "lost."
- The rightmost bits shifted into the register are **000...00**
- It's a multiplication by  $2^{\text{positions}}$  but with limited precision.



## SHIFTING BITS RIGHT (LOGICAL)

SHIFT A REGISTER'S BITS **LEFT** SOME NUMBER OF POSITIONS

**SRL** *destination, positions*

### ▶ NOTES:

- This is a "shift logical value right"
- The bits of the ***destination*** are shifted right, with the rightmost bits "lost."
- The leftmost bits shifted into the register are **000...00**
- It's a division by  $2^{\text{positions}}$  but with limited precision, *treating the number as an unsigned value.*

## SHIFTING BITS RIGHT (ARITHMETIC)

SHIFT A REGISTER'S BITS **RIGHT** SOME NUMBER OF POSITIONS

**SRA** *destination, positions*

### ▶ NOTES:

- This is a "shift arithmetic value right"
- The bits of the **destination** are shifted right, with the rightmost bits "lost."
- The leftmost bits shifted in are **sss...ss** where **s** is the sign bit.
- It's a division by  $2^{\text{positions}}$  with limited precision, *treating the number as a two's complement encoded integer.*

## SAMPLE MIPS: BITSINREVERSE.S

- ▶ This outputs the bits of a register's value, in reverse order:

```
output_loop:
    beqz    $t1, done        # if y == 0 go to done
    andi   $t0, $t1, 1      # bit = x % 2
output_bit:
    li     $v0, 1           # print(bit)
    move   $a0, $t0         #
    syscall                               #
shift_right:
    sra    $t1, $t1, 1      # x /= 2
    b     output_loop
done:
```

# SAMPLE MIPS: BITS.S

- This outputs the bits of a register's value in the correct order:

```
    li    $t2, 0x80000000    # set up the bit mask
    li    $t4, 0             # start = false
output_loop:
    beqz  $t2, done         # if mask == 0 go to done
    and   $t0, $t1, $t2     # extract the bit using the bit mask
    li    $t3, 0            # bit = 0
    beqz  $t0, after_set_1
    li    $t3, 1            # bit = 1
    li    $t4, 1            # start = true
after_set_1:
    beqz  $t4, shift_right
output_bit:
    li    $v0, 1            # print(bit)
    move  $a0, $t3         #
    syscall                #
shift_right:
    srl   $t2, $t2, 1       # shift the bit mask right
    b     output_loop
done:
```

## SCHOOLBOOK MULTIPLICATION IN BINARY

- ▶ Suppose we want to multiply 34 by 11 using binary notation:

## SAMPLE MIPS: MULTIPLY.S

- ▶ The resulting "schoolbook" code is surprisingly compact

```
multiply:
    li      $t0, 0          # product = 0
multiply_loop:
    beqz    $t2, report     # if y == 0 go to report
    andi    $t3, $t2, 1     # bit = y % 2
    beqz    $t3, skip       # if bit == 0 go to skip
    add     $t0, $t0, $t1   # sum += x
skip:
    sll     $t1, $t1, 1     # x *= 2
    sra     $t2, $t2, 1     # y /= 2
    b      multiply_loop
report:
```

## FUNCTION CALLS IN MIPS

The MIPS system calls hint at a more general mechanism we need, namely...

Q: How do we mimic C++'s function calling mechanism in MIPS?

A: By following the MIPS function calling conventions and stack discipline.

OUTLINE:

- ▶ SOME SIMPLE C++ EXAMPLES
- ▶ CALL/RETURN WITH **JAL/JR** ; PARAMETER PASSING
- ▶ CREATE/PUSH AND TAKE-DOWN/POP OF STACK FRAME
- ▶ EXAMINE CONVENTIONS FOR SAVING REGISTERS' VALUES ON THE FRAME

## RECALL: FUNCTIONS IN C++

► We considered this C++ program:

```
1. int two_digits(int tens, int ones) {
2.     return 10 * tens + ones;
3. }
4. int times100(int number) {
5.     return 100 * number;
6. }
7. int main(void) { int A, B, C, D;
8.     cin >> A;
9.     cin >> B;
10.    cin >> C;
11.    cin >> D;
12.    int hi = two_digits(A,B);
13.    int lo = two_digits(C,D);
14.    int n = times100(hi) + lo;
15.    cout << n << endl;
16. }
```



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2.     return 10 * tens + ones;
3. }
4. int times100(int number) {
5.     return 100 * number;
6. }
7. int four_digits(int w, int x, int y, int z) {
8.     return times100(two_digits(w,x)) + two_digits(y,z);
9. }
10. int main(void) { int A, B, C, D;
11.     cin >> A;
12.     cin >> B;
13.     cin >> C;
14.     cin >> D;
15.     cout << four_digits(A,B,C,D) << endl;
16. }
```

▶ We're going to work to convert this and the earlier example into MIPS code.

## JUMPING FOR CALL AND RETURN

▶ There are two "jump" instructions used to call and return from functions:

- **JAL** *label*

- This jumps to the callee code at that *label*.

- It saves the *return address* into register **\$ra**

- The return address is for the caller's instruction just below the **JAL**.

- **JR** **\$ra**

- This jumps from the callee back to the instruction below the call site.

- The caller then continues executing.

## SPECIAL REGISTERS IN MIPS

- ▶ There are several conventions for registers in MIPS:
  - Registers **\$a0-\$a3** hold the arguments for the call. (The first 16 bytes.)
  - Registers **\$v0-\$v1** hold the result of the call.
  - Registers **\$ra** holds the return address of the call.
  - Registers **\$fp** and **\$fp** mark the top and bottom of the **stack frame**.

## STACK FRAME DISCIPLINE

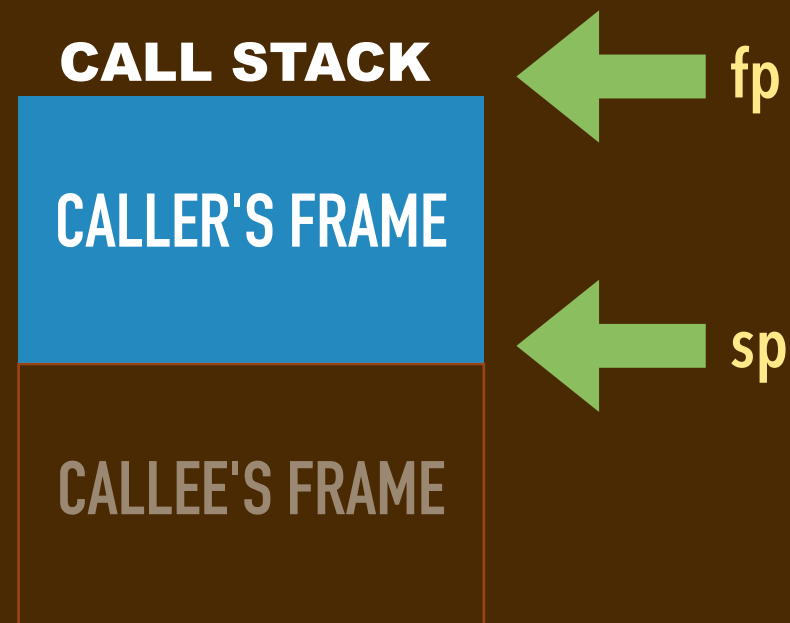
- ▶ The MIPS calling conventions designate that...
  - register **fp** points to the byte just above the top of a function's frame.
  - register **sp** points to the byte just at the bottom of a function's frame
- ▶ ...and that the callee **preserve the caller's frame**.



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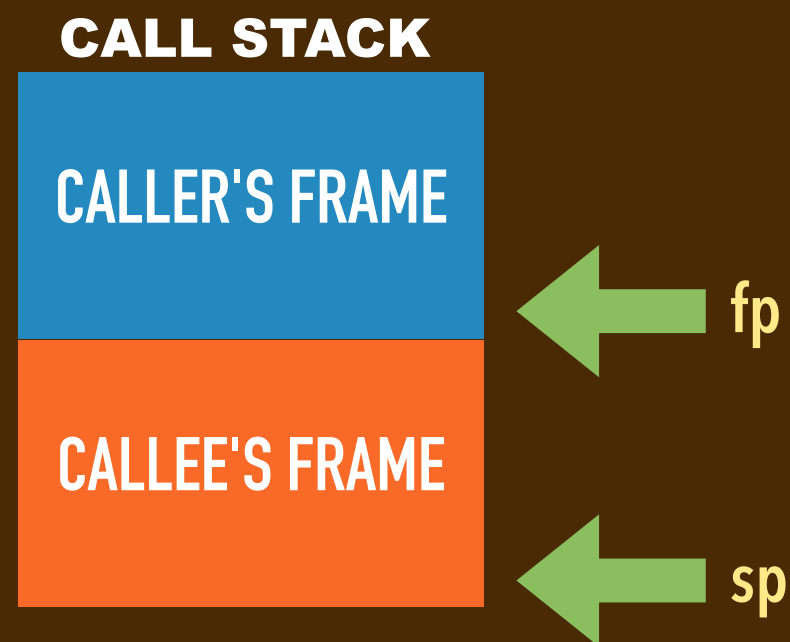
***\*BEFORE THE CALL\****



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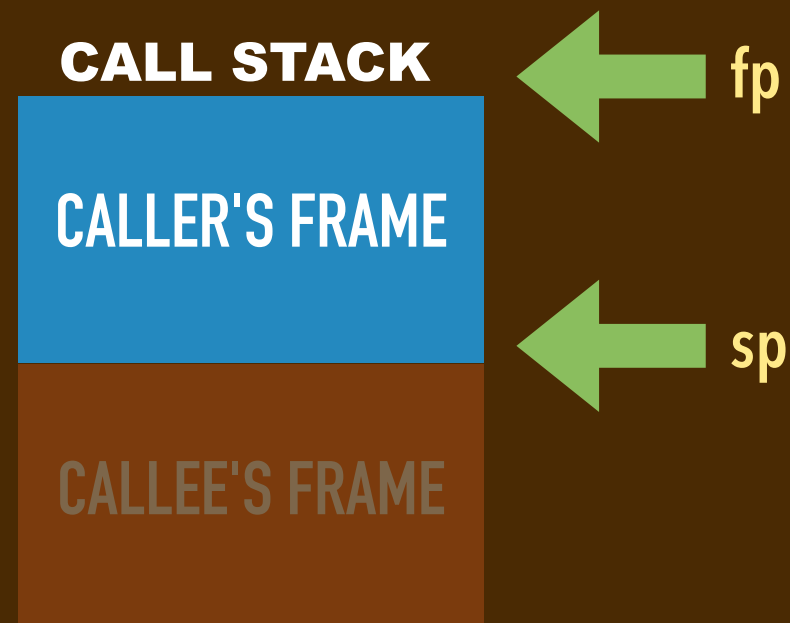
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- ▶ ...and that the callee **preserve the caller's frame**.

***\*AFTER THE CALL\****





## STACK FRAME DISCIPLINE (CONT'D)

- ▶ The MIPS calling conventions designate that...
  - the frame size should be at least 32 bytes
  - the addresses in `fp` and `sp` should be **word-aligned** (multiples of 4).
  - (some say they should be **double-word aligned** (multiples of 8))

## CODE STRUCTURE

- ▶ Every call site has a prologue and an epilogue:
  - The caller's prologue saves registers and sets up arguments.
  - Its epilogue gets the return value and restores saved registers.
- ▶ Every function's code has a prologue and an epilogue:
  - The callee's prologue sets up its frame, saves registers, grabs arguments.
  - Its epilogue restores registers, takes down the frame, sets the return value.

## CALLEE-**SAVED** REGISTERS

- ▶ The MIPS calling conventions designate that...
  - Registers need to be preserved with a function call. **No clobbering!**
- ▶ Some registers are "***callee-saved***"
  - The function called must save the values of these registers on the stack before using them.
  - It must restore their values from the stack before it returns to the caller.
  - These registers' values are guaranteed to be preserved with a function call.

## CALLER-**SAVED** REGISTERS

- ▶ The MIPS calling conventions designate that...
  - Registers need to be preserved with a function call. **No clobbering!**
- ▶ Some registers are "**caller-saved**"
  - The caller saves these on the stack before calling a function.
  - The caller restores them from the stack after the call.
  - These registers' values may not be preserved with a function call.

# FOUR\_DIGITS IN MIPS USING T REGISTERS

```
four_digits:
```

```
sw    $ra,-4($sp)
```

```
sw    $fp,-8($sp)
```

```
move  $fp,$sp
```

```
addi  $sp,$sp,-32
```

```
sw    $a2,-20($fp)
```

```
sw    $a3,-24($fp)
```

```
jal   two_digits
```

```
move  $t0,$v0
```

```
sw    $t0,-12($fp)
```

```
lw    $a0,-20($fp)
```

```
lw    $a1,-24($fp)
```

```
jal   two_digits
```

```
move  $t1,$v0
```

```
sw    $t1,-16($fp)
```

```
lw    $t0,-12($fp)
```

```
move  $a0,$t0
```

```
jal   times100
```

```
lw    $t1,-16($fp)
```

```
add   $v0,$v0,$t1
```

```
addi  $sp,$sp,32
```

```
lw    $fp,-8($sp)
```

```
lw    $ra,-4($sp)
```

```
jr    $ra
```

## MIPS CALLING CONVENTIONS SUMMARY: THE CALLER

- ▶ Before the caller calls a function...
  - It saves caller-saved registers (a0-a3, t0-t9) onto its stack frame.
  - It places the parameters into registers a0-a3.
  - It pushes 5th, 6th, etc parameters onto the bottom of its stack frame.
- ▶ Using **JAL** saves a return address to register ra.
- ▶ After the function is called...
  - The caller restores registers it has saved, if needed.
  - It extracts the return value from register v0 and v1.

## MIPS CALLING CONVENTIONS SUMMARY: THE CALLEE

- ▶ When a function is called...
  - It saves callee-saved registers (`fp`, `sp`, `ra`, `s0-s7`) onto its stack frame.
  - It extracts argument registers `a0-a3` and from slots just above its frame.
  - It normally sets `fp` to the old `sp`, subtracts an **offset** from `sp`.
    - The **offset** it chooses is the callee's **frame size**. It has to be a **multiple of 8**.
- ▶ Before a function returns...
  - It puts the return value into register `v0` and `v1`.
  - It restores registers for the caller, including `fp`, `sp`, and `ra`.
- ▶ It then performs **JR \$RA** to return control back to the caller.

# FOUR\_DIGITS IN MIPS WITH SOME CLEAN-UP

```
four_digits:
```

```
    sw    $ra, -4($sp)
```

```
    sw    $fp, -8($sp)
```

```
    move  $fp, $sp
```

```
    addi  $sp, $sp, -32
```

```
    sw    $a2, -16($fp)
```

```
    sw    $a3, -20($fp)
```

```
    jal   two_digits
```

```
    sw    $v0, -12($fp)
```

```
    lw    $a0, -16($fp)
```

```
    lw    $a1, -20($fp)
```

```
    jal   two_digits
```

```
    lw    $a0, -12($fp)
```

```
    sw    $v0, -12($fp)
```

```
    jal   times100
```

```
    lw    $t1, -12($fp)
```

```
    add  $v0, $v0, $t1
```

```
    addi  $sp, $sp, 32
```

```
    lw    $fp, -8($sp)
```

```
    lw    $ra, -4($sp)
```

```
    jr    $ra
```



## CAN SEE COMPILER BEHAVIOR ONLINE

Check out <https://godbolt.org/>