

PYTHON PROCEDURES: PASSING FUNCTIONS TO FUNCTIONS

LECTURE 03-2

PROCEDURES

FUNCTION OBJECTS AS PARAMETERS

PROJECT 1

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PROGRAMMER-DEFINED PROCEDURES

- ▶ Python has the same **def** syntax for defining **procedures**
 - This is my term for a "function that does not return a value."
 - Instead, it does some stuff, performs some actions.

- ▶ For example

```
def printBoxTop(size):  
    dashes = "-" * size  
    print("+ " + dashes + "+")  
  
def printBox(width):  
    printBoxTop(width)  
    print("| " + (" " * width) + "|")  
    printBoxTop(width)
```

- ▶ Below is its use. It's as if we've invented a **printBox** statement.

```
>>> printBox(4)  
+----+  
|    |  
+----+  
>>>
```

SYNTAX: PROCEDURE DEFINITION

Below gives a template for procedure definitions:

```
def procedure-name (parameter-list) :  
    lines of statements that compute using the parameters  
    ...  
    return
```

- ▶ The last line is often a **return** statement, but it isn't needed.
- ▶ There can also be **return** statements within the code.
 - ➔ These lead Python to exit the procedure as soon as they are reached.
 - ➔ Control returns back to where the procedure was called, continues there.

EXAMPLE SCRIPT WITH PROCEDURES

```
def printBoxTop(size):  
    dashes = "-" * size  
    print("+ " + dashes + "+")  
  
def greetTheUser(name):  
    print("Hi, " + name + ". Nice to meet ya!")  
  
def printBox(w):  
    printBoxTop(w)  
    print("|" + (" " * w) + "|")  
    printBoxTop(w)  
  
user = input("What's your name? ")  
greetTheUser(user)  
print("I'd like to make you a box.")  
width = int(input("How wide of a box would you like? "))  
printBox(width)  
print("Here is one that is twice as wide:")  
printBox(width * 2)
```

PROCEDURES RETURN THE **NONE** VALUE

- ▶ All three of these procedures do the exact same thing:

```
def greetThenReturn_version1(name):  
    print("Hi, " + name + ".")
```

```
def greetThenReturn_version2(name):  
    print("Hi, " + name + ".")  
    return
```

```
def greetThenReturn_version3(name):  
    print("Hi, " + name + ".")  
    return None
```

- ▶ The first implicitly returns **None**. The first explicitly returns but implicitly returns **None**. The third explicitly returns the **None** value.

NONE IS WEIRDLY HANDLED BY THE PYTHON INTERPRETER

- ▶ Here is some fun with **None**, and with procedures (that return **None**):

```
>>> print("hello")
hello
>>> print(None)
None
>>> "hello"
'hello'
>>> None
>>> 3+4
7
>>> print(print("hello"))
hello
None
>>> greetThenReturn("Jim")
Hello, Jim.
>>> print(greetThenReturn("Jim"))
Hello, Jim.
None
```

FUNCTIONS VS. PROCEDURES

► **"Function":**

- A function gets passed some parameters, executes, and then returns a result.
- A function is used within an expression.

► **"Procedure":**

- A procedure is something that (typically) performs some action/work but does not return a value.
- A procedure is used as a statement of a line of code.
- When a procedure's work is done, Python continues executing after the line where it was called. (Control "jumps" then returns.)

FUNCTIONS VS. PROCEDURES (CONT'D)

- ▶ In Python, procedures are really just functions.
 - Python doesn't distinguish procedures from functions.
 - This is just my personal dichotomy, from older languages (Pascal, C).
 - ➔ Functions can perform actions (print, get input) too, before they return.

PASSING FUNCTIONS TO FUNCTIONS

LECTURE 03-2

INTRO TO HIGHER ORDER FUNCTIONS

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FUNCTION OBJECTS

We've seen some evidence that Python treats functions like data

```
>>> def square(x):
...     return x * x
...
>>> square
<function square at 0x104cbb7e0>
>>> type(square)
<class 'function'>
>>> def abs(x):
...     if x < 0:
...         return -x
...     else
...         return x
...
>>> abs
<function abs at 0x104cbb880>
>>> type(abs)
<class 'function'>
>>>
```

FUNCTION VARIABLE ASSIGNMENT

You can assign (and reassign) variables to functions

```
>>> f = square
>>> g = abs
>>> f
<function square at 0x104cbb7e0>
>>> g
<function abs at 0x104cbb880>
>>> f(-3)
9
>>> g(-3)
3
>>> g = f
>>> g
<function square at 0x104cbb7e0>
>>> g(-3)
9
>>>
```

FUNCTION VARIABLES IN A SCRIPT

This can be quite powerful. Here is a script that uses one:

```
def square(x): return x * x
def cube(x): return x ** 3

print("Which function would you like to apply?")
which = input("Enter 'square' or 'cube': ")
if which == "square":
    f = square
else:
    f = cube

x = int(input("Enter the function's input: "))

y = f(x)
print(which + "(" + str(x) + ") is " + str(y))
```

THE HIGHER-ORDER FUNCTION FEATURES OF PYTHON

Python treats function as data objects. This gives Python certain nifty features.

Generally:

Languages that have *higher-order function features* allow you to:

- ▶ Assign variables to be function objects,
- ▶ Pass functions/procedures as arguments to other functions/procedures.

EXAMPLE: FINDING A MINIMUM VALUE

- ▶ **Given:** the polynomial $p(x) = x^4 - 8x^3 + 6x - 4$
- ▶ **Find:** which integer from 3 to 10 yields the lowest value?

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- ▶ **Given:** the polynomial $p(x) = x^4 - 8x^3 + 6x - 4$
- ▶ **Find:** which integer from 3 to 10 yields the lowest value?

Here is a script that computes that minimum:

```
def p(x):  
    return x**4 - 8*x**3 + 6*x - 4  
  
min_so_far = p(3)  
where_seen = 3  
i = 4  
while i <= 10:  
    if p(i) < min_so_far:  
        min_so_far = p(i)  
        where_seen = i  
    i = i + 1  
print(where_seen)
```

A TEMPLATE FOR FINDING MINIMUMS

Note that there is a **template** for performing this algorithm. Can work for...

- ✦ *...any function*
- ✦ *...any start value*
- ✦ *...any end value*

```
min_so_far = some_function(3)
where_seen = start
i = start + 1
while i <= end:
    if some_function(i) < min_so_far:
        min_so_far = some_function(i)
        where_seen = i
    i = i + 1
print(where_seen)
```

EXAMPLE: FINDING A MINIMUM VALUE

The code below **generalizes** on the **range** we check:

```
def p(x):  
    return x**4 - 8*x**3 + 6*x - 4  
  
def argument_for_min_p(start, end):  
    min_so_far = p(start)  
    where_seen = start  
    i = start + 1  
    while i <= end:  
        if p(i) < min_so_far:  
            min_so_far = p(i)  
            where_seen = i  
        i = i + 1  
    return where_seen  
  
print(argument_for_min_p(3, 10))  
print(argument_for_min_p(-20, 5))  
print(argument_for_min_p(387, 501))
```

EXAMPLE: FINDING A MINIMUM VALUE

The code below **also generalizes** on the *function being checked*:

```
def p(x):  
    return x**4 - 8*x**3 + 6*x - 4  
  
def argument_for_min(some_function, start, end):  
    min_so_far = some_function(start)  
    where_seen = start  
    i = start + 1  
    while i <= end:  
        if p(i) < min_so_far:  
            min_so_far = some_function(i)  
            where_seen = i  
        i = i + 1  
    return where_seen  
  
print(argument_for_min(p, 3, 10))  
print(argument_for_min(p, -20, 5))  
print(argument_for_min(p, 387, 501))
```

EXAMPLE: USING IT FOR TWO DIFFERENT FUNCTIONS!

```
def argument_for_min(some_function, start, end):  
    min_so_far = some_function(start)  
    where_seen = start  
    i = start + 1  
    while i <= end:  
        if p(i) < min_so_far:  
            min_so_far = some_function(i)  
            where_seen = i  
        i = i + 1  
    return where_seen
```

```
def p(x):  
    return x**4 - 8*x**3 + 6*x - 4
```

```
def another(arg):  
    return 3*arg**5 - 100*arg**2 + 99
```

```
print(argument_for_min(p, 3, 10))  
print(argument_for_min(another, 3, 10))
```

HIGHER ORDER FUNCTIONS

- ▶ Python treats functions as objects.
 - This means we can hand functions to other functions.
 - ✦ Functions can be passed as parameters.
- ▶ Functions that take functions as parameters are ***higher order functions***.

A HIGHER-ORDER PROCEDURE

Let's invent a procedure that reports a function's value

```
def report_eval(name, f, x):  
    ????
```

Here is how I'd like it to work:

```
>>> report_eval("abs", abs, -5)  
The value of abs(-5) is 5.  
>>> report_eval("abs", abs, 3)  
The value of abs(3) is 3.  
>>> report_eval("square", square, -5)  
The value of square(-5) is 25.  
>>> report_eval("square", square, 3)  
The value of square(3) is 9.
```

A HIGHER-ORDER PROCEDURE

This procedure reports a function's value:

```
def report_eval(name, f, x):  
  
    # evaluate f at x  
    y = f(x)  
  
    # build the report string  
    it = name + "(" + str(x) + ")"  
    that = str(y)  
    s = "The value of " + it + " is " + that + "."  
  
    # output the report string  
    print(s)
```

Here is it in use:

```
>>> report_eval("abs", abs, -5)  
The value of abs(-5) is 5.  
>>> report_eval("square", square, 3)  
The value of square(3) is 9.
```

ANOTHER HIGHER-ORDER PROCEDURE

How about this procedure?

```
def natfun_report(name, natfun, n):  
    ????
```

Here is how I'd like it to work:

```
>>> sequence_report("square", square, 9)
```

n		square(n)
1		1
2		4
3		9
4		16
5		25
6		36
7		49
8		64
9		81

A SEQUENCE REPORTER

Here is the code for it:

```
def natfun(name, natfun, n):  
    print(" n | " + name + "(n)")  
    print("-"*3 + "+" + "-"* (len(name)+5))  
    i = 1  
    while i <= n:  
        print(" "+str(i)+" | "+str(natfun(i)))  
        i = i + 1
```

ANOTHER HIGHER-ORDER PROCEDURE

Q: What does this procedure do?

A: ?

```
def abcde(op, size):  
    i = 1  
    while i <= size:  
        j = 1  
        while j <= size:  
            value = op(i, j)  
            print(str(value), end='\\t')  
            j = j + 1  
        print()  
        i = i + 1
```

A MULTIPLICATION TABLE

This is what it does:

```
>>> def multiply(x,y):  
...     return x * y  
...
```

```
>>> abcde(multiply,5)
```

1	2	3	4	5
2	4	6	8	10
3	6	9	12	15
4	8	12	16	20
5	10	15	20	25

A MULTIPLICATION TABLE

This is what it does:

```
>>> from operator import mul
```

```
>>> abcde(mul,5)
```

1	2	3	4	5
2	4	6	8	10
3	6	9	12	15
4	8	12	16	20
5	10	15	20	25

ANOTHER HIGHER-ORDER PROCEDURE

Q: What does this procedure do?

A: It produces a table for any two-parameter function **op**.

```
def table(op, size):  
    i = 1  
    while i <= size:  
        j = 1  
        while j <= size:  
            value = op(i, j)  
            print(str(value), end=' \t ' )  
            j = j + 1  
        print()  
        i = i + 1
```

HIGHER-ORDER FUNCTION FEATURES

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- ▶ Pass functions/procedures as arguments to other functions/procedures. ✓
- ▶ Return functions back from other functions, *and*
- ▶ Express functions succinctly and anonymously (using `lambda`).

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- ▶ Pass functions/procedures as arguments to other functions/procedures. ✓
- ▶ Return functions back from other functions, *and*
- ▶ Express functions succinctly and anonymously (using `lambda`).

We will talk about these features later.

PROJECT 1

AUTOMATING A DICE STRATEGY GAME

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